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9 **Tree density and stand age effects on allometric equation development and**
10 **biomass partitioning in lodgepole pine forests near Yellowstone National**
11 **Park, WY**
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1 **Abstract**

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3 Allometric equations that estimate biomass for various tree components are often
4 sensitive to geographic location, as well as differences in tree age and stand density within a
5 given area. We developed new allometric equations for predicting above- and belowground
6 biomass of mature lodgepole pine (*Pinus contorta* var. *latifolia* (Engelm. ex Wats.) Critchfield)
7 in the Greater Yellowstone Ecosystem (GYE) in three stands that differed in stand age and tree
8 density using standard harvest techniques. We compared our new equations to lodgepole pine
9 allometrics developed in other areas to evaluate their usefulness; we also tested the utility of
10 equations developed previously in the GYE for young, postfire saplings for predicting biomass
11 of mature trees. Finally, we evaluated the influence of stand age and tree density on biomass
12 partitioning in the three stands. R-squared values for the nine equations developed in this study
13 ranged from 0.92 - 0.98, and diameter at breast height (dbh) was the primary predictor for all
14 nine models. The influence of stand age and tree density was variable for individual
15 aboveground and belowground biomass components; however, equations that predict total tree
16 and total aboveground biomass were not influenced by either age or density. Allometric
17 equations developed for lodgepole pine elsewhere - in southeastern Wyoming and British
18 Columbia – consistently produced poorer estimates of biomass for mature lodgepole pine in the
19 GYE, supporting the idea that many allometric relationships in forested systems are site-specific.
20 Similarly, equations developed for young saplings in the GYE did not accurately predict the
21 biomass of mature trees, nor did our new equations adequately predict biomass of young, postfire
22 saplings. Proportionately, all aboveground tree biomass components were significantly higher in
23 the young, sparse stand than in the young, dense or old, sparse stands, suggesting an influence of
24 both density and age. The young, dense stand showed significantly higher total aboveground

1 biomass partitioning and significantly lower total root biomass than either of the sparse stands.
2 Overall biomass partitioning patterns were more similar between the young, dense and old,
3 sparse stand (bole > fine fuels > total coarse root > branches) than the young, sparse stand (bole
4 > fine fuels > branches > total coarse root biomass). While some recent studies have suggested
5 using a universal, functional approach for estimating total forest biomass, our study demonstrates
6 measurable and significant differences among allometric equations developed in the Rocky
7 Mountains for a single tree species, supporting the continued development of these kinds of
8 predictive tools.

9

10 Keywords: allometric equations; lodgepole pine; Yellowstone; biomass

1 **Introduction**

2 The ability to relate easily measured tree characteristics, such as diameter and height, to
3 total tree biomass and individual component biomass is an important statistical and management
4 tool. For example, forest managers may use this information when investigating relationships
5 between forest productivity and stand density, to measure woody fuel amounts (Agee 1983), or
6 to estimate carbon accumulation and storage in forested systems (e.g., Giardina and Ryan 2002).
7 It is often difficult, if not impossible, for managers or researchers to develop biomass equations
8 for each project in which they are involved, and must often rely on existing equations to provide
9 biomass estimates (Crow 1988). However, largely because of geographic and physiographic
10 differences among study areas, biomass equations are not universally applicable and models
11 developed in a particular area may not be appropriate across the range of an individual tree
12 species, even if many may already exist.

13 Allometric equations for estimation of above- and belowground biomass of mature
14 lodgepole pine (*Pinus contorta* var. *latifolia* (Engelm. ex Wats.) Critchfield) trees have been
15 developed in Alberta, Canada by Johnstone (1971), in southeastern Wyoming by Pearson et al.
16 (1984), in southeastern British Columbia by Comeau and Kimmins (1989), and in Washington
17 and Oregon by Gholz et al. (1979). More recently, allometric equations for predicting biomass
18 in young, post-fire forests have also been developed in Yellowstone National Park (YNP) for
19 aboveground biomass by Turner et al. (2004) and for belowground biomass by Litton et al.
20 (2003). Despite the robust nature of most allometric equations, these previous studies have
21 suggested that they may not be universally applicable in stands of varying densities, ages, and
22 site qualities. For example, Johnstone (1971) identified a need to consider stand density and age
23 when he developed allometric models for 100-year-old lodgepole pine in Alberta, Canada.

1 Later, Pearson et al. (1984) suggested that differences in stand density, age, and site quality may
2 have caused considerable variability in tree crown biomass, and both Pearson et al. (1984), and
3 Comeau and Kimmins (1989) found that the foliage biomass: sapwood area ratio decreased with
4 increasing stand density. Such variability among sites suggests that allometric relationships are
5 also likely to differ among geographic locations due to differences in substrate, topography, and
6 climate. Keyes and Grier (1981) found that Douglas-fir had proportionately more total root
7 biomass on a low productivity site than on a high productivity site, and Comeau and Kimmins
8 (1989) found that belowground production represented a greater proportion of total production in
9 two xeric sites compared to two mesic sites.

10 Although Litton et al. (2004) and Tinker and Knight (2000) have suggested that
11 allometric models developed by Comeau and Kimmins (1989) or Pearson et al. (1984) could be
12 appropriate for use in the GYE, this may not be true. During the study by Litton et al., the
13 equations of Comeau and Kimmins and Pearson et al. were tested on only five mature trees in a
14 single stand, and did not account for variability in stand density and age. In addition, allometric
15 equations from these two studies for predicting belowground biomass in mature stands were not
16 evaluated. In fact, in general, because of methodological inconsistencies, along with site-specific
17 differences in tree density and stand age, using existing allometric equations outside the areas
18 where they have been developed often produce inconsistent biomass estimates (Peichl and Arain
19 2007; Wang et al. 2000; Jenkins et al. 2003; Tateno et al. 2004). Therefore, new allometric
20 models specific to mature forests of the Greater Yellowstone Ecosystem are needed that consider
21 differences in lodgepole pine biomass, which may vary with tree density and stand age. In this
22 study, we developed new allometric models for predicting above and belowground biomass in
23 mature lodgepole pine forests of the GYE.

1 The specific objectives of this study were to: (1) develop allometric equations for
2 predicting above and belowground biomass of mature lodgepole pine trees in the GYE,
3 accounting for differences in stand density and age; (2) compare allometric equations developed
4 in this study to allometric equations developed in other locations and equations developed for
5 young trees in YNP to determine model variability and applicability across geographic locations
6 and age classes, independent of forest structure; and (3) to determine how patterns of above and
7 belowground biomass partitioning for trees in three mature lodgepole pine stands of the GYE
8 vary with stand age and density.

9 **Methods**

10 11 *Study Areas*

12 The two study areas were located in the Caribou-Targhee National Forest (CTNF), one
13 bordering the western boundary of YNP, near Island Park, ID, and the other near the southern
14 boundary of YNP; both sites are dominated by lodgepole pine. Allometric equations were
15 developed in three lodgepole pine stands (two near Island Park and one near YNP) on the CTNF
16 that represented two age classes and two density classes. Elevations in the three stands ranged
17 from 1,951 m to 2,249 m (Table 1). In the young (~65 years old) age class, two stands of
18 different densities were examined; one young, dense (YD - 2,452 trees/ha) and the other young
19 and sparse (YS - 725 trees ha⁻¹). A single sparse (674 trees ha⁻¹) stand was sampled in the older
20 age class (OS) (~165 years old), because older stands typically have low tree densities,
21 regardless of their initial tree density (Kashian et al. 2005).

22 All three sites were located on the Koffgo soil series, consisting of loamy-skeletal, mixed,
23 superactive Vitrandic Cryochrepts. Parent material was local residuum, colluvium, or alluvium
24 developed from volcanic ash, igneous rocks, and loess (Bowerman et al. 1999). Average annual

1 precipitation was $\sim 115 \text{ cm yr}^{-1}$ in the oldest stand and $\sim 75 \text{ cm yr}^{-1}$ in the younger stands (Dirks
2 and Martner 1982). All sites were located at least 50 m from the road to facilitate equipment
3 hauling, yet avoiding road influences. Stand basal area was determined using six variable radius
4 plots in each stand (Avery and Burkhart 1994). Stand basal area was similar between the OS
5 ($16.84 \text{ m}^2 \text{ ha}^{-1}$) and YS stands ($19.71 \text{ m}^2 \text{ ha}^{-1}$), but was quite different for the YD stand (28.32
6 $\text{m}^2 \text{ ha}^{-1}$; Table 1).

7 ***Field and Lab Methods***

8 All aboveground tree biomass was harvested from a total of 46 trees within the three
9 stands, and 24 root systems were excavated to develop allometric equations between easily
10 measurable tree characteristics (e.g., dbh, tree height) and above- and belowground tree biomass
11 components. Fourteen and 15 trees were harvested in the YD stand and the YS stand,
12 respectively, and 17 trees were harvested in the OS stand. Five root systems were excavated in
13 each of the YS and OS stands and 14 root systems were harvested in the YD stand.

14 In each stand, trees were harvested along each of three 25-m transects. Trees were
15 selected at 5m intervals along each transect to represent the range of tree sizes found for trees in
16 their respective stands. Trees with unusually poor tree form, excessive mistletoe, or any defect
17 that could alter the biomass of the tree, such as heart rot or insect damage, or any tree outside of
18 the acceptable age range (≤ 15 years of the oldest tree in the stand) were avoided.

19 Prior to harvest, DBH (diameter at breast height, 1.37 m) was measured and crown width
20 was estimated using a meter tape. After felling of the tree, total height and height to live crown
21 base were measured. Crown base was defined as the point along the bole at the bottom of
22 roughly 90% of the crown mass. Crown length was calculated as:

1 annual foliage biomass. All fine fuels were weighed, and a random subsample was taken from
2 each crown section to determine moisture content. We then removed all remaining needles from
3 the twigs and weighed them separately to determine foliage biomass.

4 Belowground Components

5 The entire coarse root system (>10mm diameter) was excavated for 24 trees with a
6 backhoe or portable winch. Prior to excavation, smaller roots (~ 10-20 mm) that could
7 potentially be damaged by the backhoe or other excavation techniques were manually removed.
8 After excavation, the root system was divided into four size classes and weighed using a digital
9 hanging scale: root crown (i.e. the massive structure directly beneath the tree bole), lateral roots
10 > 50mm in diameter, lateral roots 25-50 mm in diameter, and lateral roots 10-25 mm in diameter.
11 Subsamples from each size class were taken and weighed to determine moisture content for dry
12 weight of each size class.

13 Allometric Equation Development and Comparisons

14 We used multiple linear regression to identify relationships between measured tree
15 characteristics and the various biomass compartments described above. Rather than develop
16 equations from each stand sampled, we wanted to create equations for each tree biomass
17 component that were developed for pooled data from all three sites, but which would include
18 variables representing stand age and density. We tested a suite of tree- and stand-level measures,
19 including dbh, tree height, sapwood area, stand density and stand age, as well as all interaction
20 terms. An iterative approach was used that initially included all independent variables and their
21 interaction terms, and subsequent iterations continued until only predictor variables that were
22 significant ($p \leq 0.05$) in the model were remaining. Tree dbh was log-transformed, and we used
23 binary dummy variables for both stand age (old = 1; young = 0) and stand density (sparse = 1;

1 dense = 0). Equations that retained variables or interaction terms related to stand age or stand
2 density in the final model represent significant effects of age or density on a given biomass
3 compartment. All equation development was done using Minitab 15 (2007).

4 ***Geographic Location Comparisons*** - Equations developed for mature lodgepole pine in
5 this study were compared to equations developed by Pearson et al. (1984) for lodgepole pine in
6 the Medicine Bow Mountains of southeastern Wyoming and by Comeau and Kimmins (1989)
7 for lodgepole pine trees in British Columbia. Equations selected for comparison were developed
8 in stands that were similar in stand density and age to those developed for this study. Paired,
9 two-tailed t-tests were used to assess whether biomass estimates from this study differed
10 statistically from biomass estimates produced from the other equations ($\alpha = 0.05$). Actual
11 biomass values from this study were compared against values estimated using our allometric
12 equations to determine whether our estimated biomass values were more similar to the actual
13 values than estimated values calculated using equations developed by Pearson et al. (1984) and
14 Comeau and Kimmins (1989).

15 ***Reciprocal comparisons with equations developed for saplings in YNP*** – Estimates of
16 biomass using allometric equations developed in this study for mature trees were compared to
17 biomass measurements and estimates developed in YNP for small, young saplings for both
18 aboveground (Turner et al. 2004) and belowground (Litton et al. 2003) biomass compartments.
19 We used total biomass measures from 36 randomly selected saplings that were harvested by
20 Turner et al. (2004) during 1999 in YNP. Similarly, the equations developed by Turner et al.
21 (2004) and Litton et al. (2003) were used to estimate the respective biomass compartments for
22 mature trees harvested in this study. Paired t-tests were used to test for significant differences
23 between measured and predicted values for all comparisons. Both of these sets of comparisons

1 were done to determine the usefulness of allometric equations developed for mature trees in
2 predicting biomass of young saplings, and vice versa.

3 Tree Level Biomass Estimations

4 The dry weight biomass values for the 24 trees that were completely harvested in this
5 study (both above- and belowground components) were used to calculate biomass partitioning
6 patterns for above and belowground components of lodgepole pine trees in the three study sites.

7 *Statistical Analyses*

8 All other statistical analyses were done using SPSS 14.0 (SPSS Inc. 2005). To determine
9 whether partitioning patterns at the tree level differed as a function of density and/or age, one-
10 way ANOVAs were conducted, followed by Tukey's HSD post-hoc analyses. The following
11 variables were used for comparisons: biomass, and percent of total biomass for bole, branches,
12 foliage, needles, total coarse root, root crown, and lateral roots; the total coarse root biomass:
13 total aboveground biomass ratio was also calculated for the three stands. For these analyses, tree
14 within stand was the sample unit.

15 **Results**

16 Allometric Equation Development

17 *Equation summaries*

18 The nine linear allometric models developed for all measured tree components are shown
19 in Table 2; R^2 values ranged from 0.92 to 0.98. Plots of residuals versus dbh do not show
20 evidence of bias or excessive heteroscedasticity for any of the nine models (Figures 1 and 2). All
21 nine equations used a log-transformation of diameter at breast height (dbh) as the primary
22 predictor variable, although other predictors were used in some models. Two of the nine
23 equations – total aboveground biomass and total tree biomass - included dbh as the only

1 independent variable, and neither stand age nor density influenced these equations. Tree bole
2 biomass and fine fuels were the only two equations that were influenced by the interaction of
3 both stand age and stand density with dbh, and the fine fuels equation also included an effect of
4 stand density (Table 2). Foliage, total coarse root biomass and root crown biomass equations
5 included stand age, or its interaction with dbh, in the best models for these components, yet
6 lateral root biomass was influenced by stand density and its interaction with dbh, but not by
7 stand age (Table 2). The equation for branch biomass was the only model that included height as
8 an important predictor, and was not influenced by either stand age or stand density.

9 *Comparisons among Geographic Locations*

10 Predicted biomass values from equations developed in this study were closer to actual
11 biomass of lodgepole pine in the Greater Yellowstone Ecosystem than predicted values from
12 equations developed by Comeau and Kimmins (1989) and Pearson et al. (1984) (paired t-test,
13 $p < 0.05$; Figures 3 and 4). Predicted values applying our study's equations produced biomass
14 values that were not significantly different (paired t-test, $p > 0.05$) from actual biomass values.
15 However, estimates of branch biomass applying Pearson et al.'s equations were slightly more
16 similar to actual values (paired t-test, $p = 0.005$) than were estimated values applying our
17 equations (paired t-test, $p = 0.003$). The greatest difference in observed versus predicted biomass
18 between studies was for larger diameter trees (Figures 3 and 4), supporting the observation of
19 increased variation in allometric models with increasing tree size. Biomass estimates produced
20 by models from studies northwest (Comeau and Kimmins 1989) and southeast (Pearson et al.
21 1984) of the GYE produced significantly higher estimates of root biomass, lower estimates of
22 needle and branch biomass, and relatively comparable estimates of bole biomass (Figures 3 and

1 4). The root biomass estimates generated from models developed in the Medicine Bow
2 Mountains produced slightly higher biomass estimates than from this study (Figure 4).

3 *Reciprocal comparisons with equations developed for saplings in YNP*

4 Allometric equations developed from this study for mature trees did not perform well
5 when predicting above- or belowground biomass for young, postfire saplings in YNP. Our
6 equations significantly overestimated total aboveground biomass ($p < 0.0001$), compared to
7 measured values, and the range of predicted biomass values (41 – 35, 068 g) was over three
8 times higher than the measured values (3 – 10,565 g; Figure 5a). Our equations also
9 significantly overestimated total coarse root biomass ($p < 0.0001$), when compared to measured
10 values, and the range of predicted values (4 – 2,566 g) was again over threefold larger than the
11 measured values (0.7 – 801 g; Figure 5b).

12 Similarly, allometric equations developed by Turner et al. (2004) and Litton et al. (2003)
13 for young, postfire saplings significantly underestimated both above- and belowground biomass
14 for mature trees ($p < 0.001$; Figure 3).

15 Age and Density Effects on Biomass Partitioning Patterns

16 Mean total tree biomass was greatest in the OS stand, as expected, but not significantly
17 greater than in the YS stand (Table 3). However, the mean total tree biomass of both sparse
18 stands, regardless of age, was significantly higher than the young, dense stand ($p < 0.001$; Table
19 3). This allocation pattern was similar for three of the four aboveground biomass components;
20 branches, fine fuels, and needles in both the OS and YS stands were significantly higher than the
21 YD stand, but were not significantly different from each other. Mean bole biomass, on the other
22 hand was significantly higher in the old stand than the two younger stands ($p < 0.001$; Table 3).

1 Mean total root biomass and lateral root biomass per tree were both significantly lower in the YD
2 stand than either the OS or YS stands ($p < 0.001$; Table 3).

3 When expressed as a proportion of total tree biomass, mean total aboveground biomass
4 per tree was similar among the three sites, but was significantly higher in the YD stand (90.5%)
5 than in the OS or YS stands (84.5% and 87.7%, respectively; Table 3). Tree boles were the
6 largest individual biomass component for all three stands, but these values were highly variable
7 among the three sites. Proportionately, all aboveground tree biomass components were
8 significantly higher in the YS stand than in the YD and OS stands (Table 3). Both sparse stands
9 showed proportionately higher total root biomass than the YD stand, but all stands showed
10 higher root crown biomass than lateral root biomass.

11 The hierarchy of biomass partitioning for the OS and YD stands was bole > fine fuels >
12 total coarse root biomass > branches; for the YS stand it was bole > fine fuels > branches > total
13 coarse root biomass (Table 3). The total root: total aboveground biomass ratio was highly
14 variable among the three sites, and ranged from a mean value of 0.11 in the YD stand to 0.19 in
15 the OS stand. The OS and YS stands were not significantly different from each other, but only
16 the OS stand ratio was significantly higher than the YD stand ($p < 0.05$; Table 3).

17 **Discussion**

18 Allometric Equation Development

19 The absence of bias for our equations suggests that they work well for lodgepole pine
20 across the range of tree diameters measured in this study (Figures 1 and 2). Diameter at breast
21 height (dbh; log transformed) was the primary morphological predictor of all biomass
22 components for this study, although stand age and density influenced some relationships.
23 Interestingly, tree height only proved to be a secondary, significant predictor of branch biomass,

1 which was surprising (Table 2). Typically, a tree's ability to produce stemwood biomass, a
2 major component of tree bole and total aboveground biomass, is often influenced by site
3 productivity (Barnes et al. 1998). Therefore, a model that includes tree height, a variable relating
4 more strongly to site productivity than any other measured parameter (Barnes et al. 1998), can
5 often explain a large amount of the variability in bole and total aboveground biomass, although
6 that was not the case in this study. Our three sites were similar with respect to site productivity,
7 perhaps explaining the lack of importance of height in our equations.

8 Notably, our equations that predict both total aboveground biomass and total tree biomass
9 were predicted by dbh alone, and were not influenced by either stand age or tree density (Table
10 2). One plausible explanation for this pattern is that stand densities may not have been different
11 enough for some of the models to differ according to stand density or to be less different than for
12 models pooled by age. Although 2,452 trees ha⁻¹ was considered in this study to be a dense
13 stand, "dog-hair" stands of mature lodgepole pine that are of comparable age can sometimes
14 reach densities higher than 10,000 trees ha⁻¹ (Koch 1996). Kashian et al. (2005), in their study of
15 stand structural development in YNP, identified two such stands that were less than 100 years
16 old, however, such stands are rare in the GYE. It is unclear whether our equations would prove
17 to be as robust in predicting various biomass compartments in very dense stands such as these.
18 On the other hand, Peichl and Arain (2007) also found that a single allometric equation was
19 effective in predicting total aboveground, belowground, and total tree biomass for eastern white
20 pine (*Pinus strobus* L.) across a range of stand ages in Ontario, suggesting that allometric
21 equations that include some form of tree diameter (dbh, basal diameter) are very useful and
22 robust.

1 Total coarse root biomass (>10 mm) and root crown biomass were best predicted by dbh
2 and either age, or the interaction with age and dbh (Table 2), whereas lateral roots were
3 influenced by tree density and its interaction with dbh. Similarly, Litton et al. (2003) also found
4 no significant influence of tree density on equations predicting total coarse root biomass in ~13-
5 yr old stands of lodgepole in YNP, and a diameter metric (basal diameter) was also the most
6 effective predictor of this component.

7 *Differences between Geographic Locations*

8 Differences in allometric equations among geographic locations are likely attributed to
9 differences in soil, topography, and climate. The soils on which Pearson et al. (1984) developed
10 allometrics in the Medicine Bow Mountains were generally less infertile and were derived
11 primarily from glacial till and fluvial conglomerates, while soils in British Columbia were Orthic
12 Eutric Brunisols for xeric sites and Brunisolic Gray Luvisols for mesic sites (Comeau and
13 Kimmins 1989). In contrast, soils of this study were more infertile and were developed on
14 volcanic substrates (Bowerman et al. 1999).

15 Predicted bole biomass was the tree component that differed the least between the GYE
16 and the Medicine Bow Mountains (Pearson et al. 1984), and was also the component most
17 similar between the GYE and British Columbia (Comeau and Kimmins 1989), suggesting that
18 relationships between bole biomass and its predictor(s) (tree diameter and/or total height) may be
19 relatively constant across gradients of elevation, topography, climate, and site productivity.

20 Needle biomass estimates derived from equations developed in southeastern Wyoming
21 (Pearson et al. 1984) and British Columbia (Comeau and Kimmins 1989) were lower than actual
22 and predicted biomass from sites in this study (Figures 3 and 4), although less so for southeastern
23 Wyoming. Conversely, root biomass in the GYE was over-predicted by equations developed in

1 British Columbia and southeastern Wyoming. This suggests that coarse root biomass has little
2 impact on the trees ability to uptake water and nutrients, because less coarse root biomass should
3 have been needed to uptake water and nutrients in British Columbia and southeastern Wyoming,
4 which are more productive sites than the GYE. However, a portion of this difference could also
5 be attributed to differences in the definition of a root crown between studies. For this study, a
6 root crown was the portion of the coarse root system that is directly below the basal swell of the
7 tree bole and within the lateral extent of the diameter of the tree at ground level. In contrast,
8 Pearson et al. (1984) defined the root crown as the structure directly below the basal swell of the
9 tree bole extending laterally to a distance of $1.5 \times \text{DBH}$.

10 The greatest differences in the biomass of tree components among geographic locations
11 occurred for larger trees (Figures 3 and 4), suggesting that differences in site conditions may
12 become increasingly important as forests become older and trees become taller. This is
13 attributed to an increase in nutrient limitation (Berger et al. 2004; Ryan et al. 1997; Smith and
14 Resh 1999; Smith and Long 2001), hydraulic limitation (Ryan and Yoder 1997), and potential
15 changes in carbon balance (Ryan et al. 1995) with increases in stand age and tree height.

16 Biomass Partitioning Patterns

17 *Aboveground Biomass*

18 Allocation to tree boles was lowest in the YS stand at the individual tree level, while bole
19 allocation to the OS and YD stands were surprisingly comparable to each other. The low
20 proportion of total tree biomass for boles in the YS stand is likely attributed to a high proportion
21 of branch and foliage biomass due to its young age and open-grown stand structure. The
22 similarity in allocation to tree boles between the OS and YD stands may be related to their
23 competitive similarity. Although not quantified, our observations suggested both of these stands

1 exhibited crown closure, yet the YS stand seemed to show lower crown density. The observed
2 increased biomass found in boles in the dense and older stands with greater crown competition
3 was consistent with the results of Nilsson and Albrekston (1993) and Kaufmann and Ryan
4 (1986). They found that tree bole biomass was greater than foliage biomass for competitively
5 suppressed trees. Future studies should include more direct measurements of competition among
6 trees, such as nearest neighbor analyses. Ryan et al. (1997) suggested that young trees allocate
7 more resources to foliage rather than to woody components, and this trend becomes less
8 pronounced with crown closure. This is supported by the results of this study, as the open-grown
9 YS stand had 22.3% of total aboveground biomass allocated to foliage, while the OS stand with
10 greater observed crown closure had 10.9% of total biomass allocated to foliage (Table 3). In
11 fact, on average, trees in the YS stand had higher branch, fine fuels, and foliage biomass than the
12 OS stand, as well as higher proportions of these components.

13 *Below: Aboveground Biomass Ratio*

14 For this study, below: aboveground biomass was found to vary as a function of both stand
15 age and tree density (Table 3). Our two sparse stand (old and young) did not differ significantly
16 from each other, nor did the two young stands (sparse and dense), but the ratio in the old, sparse
17 stand was significantly higher than the young, dense stand (Tale 3), indicating that both stand
18 density and age had an important effect on allocation to coarse root biomass. Although there are
19 some similarities in the ratio of below: aboveground biomass among sites, especially at the stand
20 level, biomass partitioning within above and belowground components was found to be highly
21 variable with stand density and age. This is similar to findings by Litton et al. (2004), who found
22 that carbon pools in young and old lodgepole pine stands in YNP were indeed influenced by tree
23 age and stand density over time following disturbance.

1 **Conclusions**

2 While some recent studies (e.g., Pilli et al. 2006; Zianis and Mencuccini 2004; West et al.
3 1999) have suggested a move towards a universal, functional approach to estimating total forest
4 biomass, rather than an empirical approach used by this study, others believe that equations for
5 predicting biomass at the tree level provide more accurate estimates than models that integrate
6 biomass components using a common scalar (e.g., Bokma 2004; Kozlowski and Konarzewski
7 2004). Our research demonstrates measurable and significant differences among allometric
8 equations developed in the Rocky Mountains for a single tree species, supporting the continued
9 development of these kinds of predictive tools. Indeed, Litton et al. (2003), along with this
10 study, identified a need for independent allometric models for young, developing saplings, rather
11 than using equations developed for mature trees, even within the same study area. However,
12 additional work is needed to determine when it is appropriate to use each set of equations and to
13 determine when the relationships between biomass and tree morphological characteristics
14 change.

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1 **Figure Captions**

2

3 Figure 1. Residual values (observed minus predicted values) of log-transformed linear equations
4 for aboveground biomass components in three lodgepole pine stands from this study as a
5 function of tree diameter at breast height.

6

7 Figure 2. Residual values (observed minus predicted values) of log-transformed linear equations
8 for belowground biomass components in three lodgepole pine stands from this study as a
9 function of tree diameter at breast height.

10

11 Figure 3. Comparison of biomass values among those directly measured by this study, those
12 predicted by this study's allometric models, and those predicted by Comeau and Kimmins'
13 allometric models.

14

15 Figure 4. Comparison of biomass values among those directly measured by this study, those
16 predicted by this study's allometric models, and those predicted by Pearson et al.'s allometric
17 models.

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19 Figure 5. Comparisons of measured versus predicted values using allometric equations from this
20 study to predict (a) young, postfire sapling total aboveground biomass, and (b) sapling root
21 biomass; (c) the application of equations developed by Turner et al. (2004) for predicting
22 lodgepole sapling aboveground biomass in YNP, but shown here predicting total aboveground

- 1 biomass of mature trees, and (d) equations developed by Litton et al. (2003) for predicting
- 2 lodgepole sapling root biomass in YNP, but shown here estimating mature tree root biomass.
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1 **Table 1.** Sites for the development of allometric equations in the Greater Yellowstone
 2 Ecosystem.

Site Name	Elevation (m)	NAD 83, UTM Zone 12		Stand Age (years)	Stand Density (trees > 5cm DBH per hectare)	Stand basal area (m ² per hectare)
		Northing (m)	Easting (m)			
Grassy Lake	2249	4886015	511735	165	674	16.84
Coffee Pot	1951	4926541	472232	64	725	19.71
US 20	1951	4925932	472657	64	2452	28.32

1 **Table 2.** Allometric equations for predicting biomass (Kg) of nine different above and belowground components of *P. contorta* in the
2 Greater Yellowstone Ecosystem. Each equation produces natural log-transformed biomass estimates that must be back-transformed.
3 “Age” and “density” variables are binary (0,1); for “age”, stands ≤ 65 years are considered young (0) and stands > 65 years are
4 considered old (1). Similarly, for “density”, stands that are ≥ 1500 trees per hectare are considered dense (0), and stands < 1500 trees
5 per hectare are considered sparse (1).
6

Biomass Component	Equation	<i>n</i>	Mean, (range)	<i>R</i>² (adj.)
Total Aboveground	$-2.10 + (2.35 * \ln(\text{dbh}))$	46		0.98
Bole	$-1.80 + (2.13 * (\ln(\text{dbh})) + (0.187 * (\text{age} * \ln(\text{dbh}))) - (0.127 * (\text{density} * (\ln(\text{dbh}))))$	46		0.97
Branches	$-6.67 + (3.78 * \ln(\text{dbh})) - (0.140 * \text{HT})$	46		0.92
Fine Fuels	$-6.87 + (3.54 * \ln(\text{dbh})) + (2.35 * \text{density}) - (0.228 * (\text{age} * (\ln(\text{dbh})))) - (0.807 * (\text{density} * (\ln(\text{dbh}))))$	46		0.95
Foliage	$-6.69 + (3.30 * \ln(\text{dbh})) - (0.0229 * (\text{age} * (\ln(\text{dbh}))))$	46		0.93
Total Coarse Root	$-4.91 + (2.60 * \ln(\text{dbh})) + (2.70 * \text{age}) - (0.809 * (\text{age} * \ln(\text{dbh})))$	24		0.98
Root Crown	$-4.45 + (2.22 * \ln(\text{dbh})) + (0.450 * \text{age})$	24		0.94
Lateral Roots	$-8.30 + (3.58 * \ln(\text{dbh})) + (4.51 * \text{density}) - (1.62 * (\text{density} * \ln(\text{dbh})))$	24		0.97
Total Tree	$-1.92 + (2.32 * \ln(\text{dbh}))$	24		0.98

1 **Table 3.** Mean tree biomass (Kg) and percent of total biomass for above- and belowground components of individual trees harvested
 2 from the three stands in this study. Values are based on dry weight measurements from a total of 24 trees, representing only those
 3 trees where the entire tree was harvested. Mean percent values for bole, branches, fine fuels, and needles are proportions of total
 4 aboveground biomass; mean percent values for root crown and lateral roots are proportions of total root biomass (> 10mm diameter).
 5 Different letters for each component denote significant differences ($\alpha = 0.05$).
 6

Component Biomass	Old, Sparse			Young, Sparse			Young, Dense		
	Biomass (Kg)		Mean % of Total	Biomass (Kg)		Mean % of Total	Biomass (Kg)		Mean % of Total
	Mean	Range		Mean	Range		Mean	Range	
Total Aboveground Biomass	187.9^a	30.7 -336.4	84.5^a	128.8^a	41.7 -207.4	87.7^a	41.0^b	12.1 – 104.5	90.5^b
Bole	141.2 ^a	26.5 – 245.2	76.9 ^a	59.7 ^b	26.0 – 93.9	49.1 ^b	31.2 ^b	10.2 – 81.1	79.1 ^a
Branches	14.9 ^a	1.7 – 40.1	6.9 ^a	24.3 ^a	3.9 – 54.7	16.5 ^b	2.7 ^b	0.3 – 5.9	5.9 ^a
Fine Fuels	31.8 ^a	2.5 – 51.1	16.2 ^a	44.9 ^a	11.8 – 70.2	34.4 ^b	7.1 ^b	0.5 – 17.5	15.1 ^a
Needles	22.0 ^a	1.6 – 38.4	10.9 ^a	27.5 ^a	8.5 – 39.1	22.3 ^b	4.6 ^b	0.2 – 11.5	9.8 ^a
Total Roots (>10mm)	30.0^a	10.1 – 49.6	15.4^a	18.2^a	6.3 – 33.8	12.3^{ab}	4.5^b	0.7 – 10.5	9.5^b
Root Crown	19.0 ^a	6.6 – 35.9	61.9 ^a	10.4 ^b	3.1 – 17.1	57.2 ^a	2.6 ^c	0.6 – 5.5	63.5 ^a
Lateral Roots (>10mm)	11.0 ^a	3.4 – 23.4	38.1 ^a	7.8 ^a	3.2 – 16.6	42.8 ^a	1.8 ^b	0.1 – 5.1	36.6 ^a
Total Tree Biomass	217.9^a	40.8 - 386	100	147.1^a	48 – 241.1	100	45.5^b	13.4 - 115	100
Total Root: Total Aboveground Biomass	0.19 (0.13 – 0.33) ^a			0.14 (0.10 – 0.16) ^{ab}			0.11 (0.03 – 0.15) ^b		

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