

# 1 Options Markets

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- Types of Options
  - Stock Options – Options on individual stocks
  - Index Options – SP500 (SPX), SP100, Nasdaq-100, DJIA, R2000...  
Payoff to in-the-money put is  $(S_T - K) * \text{multiplier}$ . Usually cash settled;  
Alternative is options on ETFs.
  - Foreign Currency Options –
  - Interest Rate Options – T-bills, T-bonds, GNMA pass-throughs
  - Futures Options – Options on futures contracts; FX and commodities
  
- Terminology
  
- Markets and Payoffs
  
- Stock Splits, Exotic Options and Embedded options.
  
- Index options (see **Hull section 13.1**)

## 2 Terminology

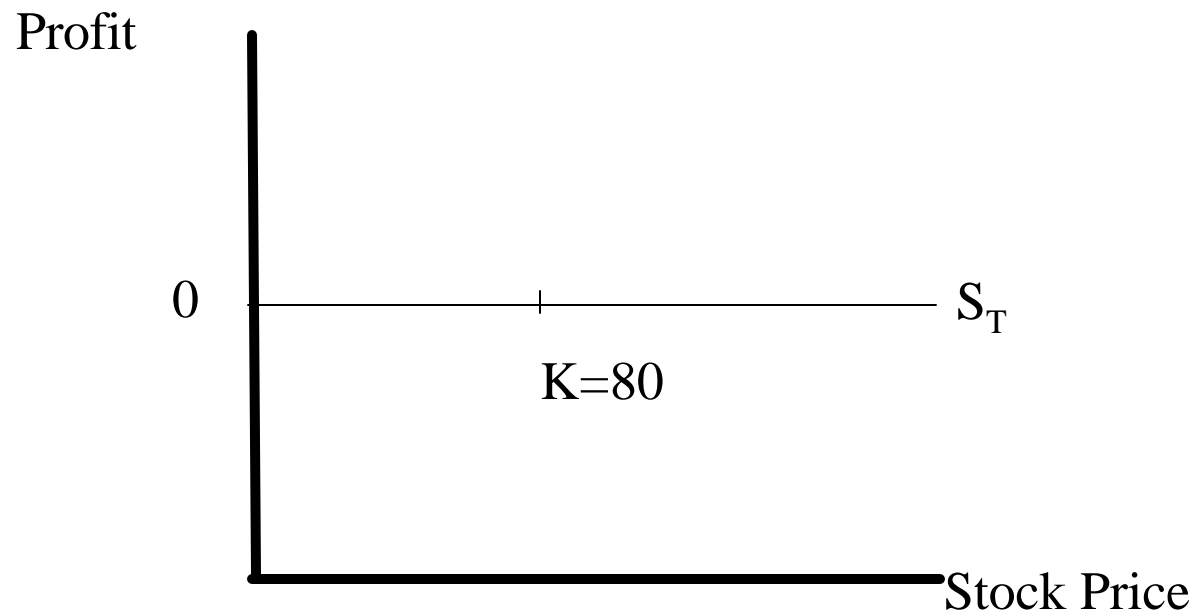
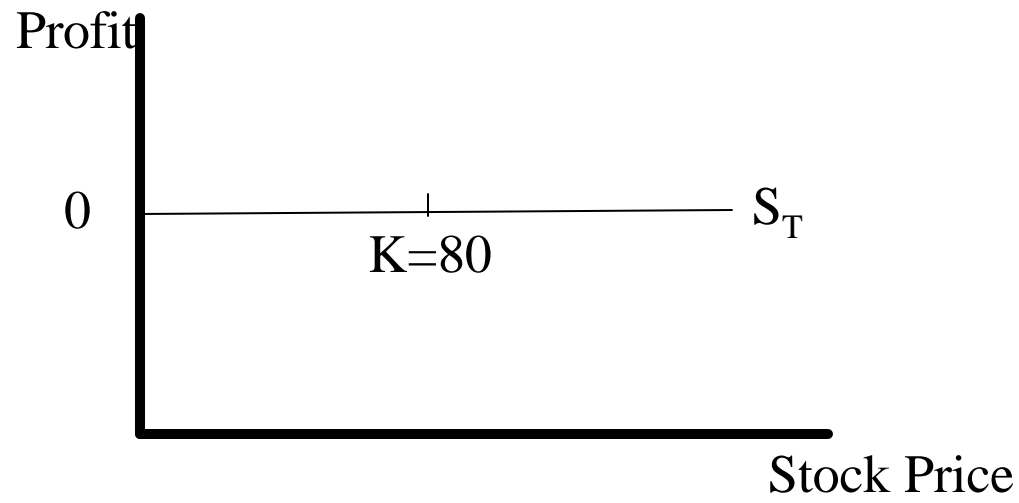
- Option - contract giving holder right, but not obligation, to buy (sell) an asset at fixed price (exercise price) at any time on or before given date (expiration date).
  - Call – right to buy.
  - Put – right to sell.
  - American – exercise any time before expiration (most common)
  - European –
  
- More
  - Intrinsic value –
  - In the Money –
  - Time value – difference between current option price and intrinsic value
  - Option class – all calls or puts on an underlying asset.
  - Option series – all options with same expiration date and strike price.
  
- Other
  - Closing positions – close position by trading into off-setting position.
  - Many brokers/exchanges auto exercise in-the-money options at expiration.
  - Margin –

### 3 Option Markets and Payoffs

- Markets – Exchanges (CBOE) standardize contracts; increase depth and liquidity
  - Strike prices set at \$2.50 or \$5 intervals; market makers post bid and ask.
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- Option Clearing Corp – Self-regulating intermediary between buyer and seller.
  - Trades cleared by OCC members (brokerages).
  - OCC assigns firms to honor exercise; sets margin requirements.
  - Writer posts margin
- Quotes – Contracts are for 100 shares, so contract costs  $price * 100$ .
  - Expire on 3<sup>rd</sup> Friday of month; Consider options  $K = \$80$ .
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| Final Stock Price ( $S_T$ ) | Payoff to Long Call             | Payoff to Long Put              |
|-----------------------------|---------------------------------|---------------------------------|
| 77                          |                                 |                                 |
| 80                          |                                 |                                 |
| 83                          |                                 |                                 |
| Payoff at $S_T$             | $\text{Max}[(S_T - K), 0]$      | $\text{Max}[(K - S_T), 0]$      |
| Profit                      | $\text{Max}[(S_T - K - C), -C]$ | $\text{Max}[(K - S_T - P), -P]$ |
| Option Written              | $\text{Min}[-S_T + K + C, +C]$  | $\text{Min}[-K + S_T + P, +P]$  |

# 4 Payoffs/Profits at Expiration



## 5 Stock Splits, Exotic Options, Embedded options

- Stock splits and stock dividends – no adjustments for cash dividends.
  - Stock dividends – OCC could adjust # shares, strike price or combination.
  - Stock split  $n$ -for- $m$  – new strike price is  $Km/n$ ; new contracts is  $Nn/m$
- Q: Consider calls on 100 shares;  $K = \$20/\text{sh}$ . Adjust terms adjust for 2-for-1 split
- A1:
- Exotic Options –
  - Asian – depend on average price of underlying asset.
  - Barrier – depend on final price and whether barrier penetrated (down and out)
  - Lookback – depend on min or max price of underlying asset.
  - Currency-translated – exercise denominated in FX.
  - Binary – fixed payoffs depending on whether some condition is met.
- Option-like securities –
  - Employee Stock Options - given to employees as part of benefits package.  
Incentive SO (VP+) vs Non-qualified SO (different tax treatment)
  - Equity in levered firm – call option, with  $K$  equal to par value of debt.  
If  $\text{assets} > \text{debt}$ , stockholders exercise option
  - Bonds –

## 6 Portfolio Insurance (1)

- Portfolio insurance – using options to “insure” value of portfolio.
  - Often use index options, most with multipliers of 100 and cash settled at exp.
  - Insuring portfolio requires choosing # puts and strike price.
  - # Puts =  $b * \$Portfolio / \$100S_0$ . Choose  $K$  for level of insurance desired.
- Q: A stock portfolio with  $b=1.0$  is currently worth \$500k and S&P500=1000. The risk-free rate is 12%/yr and div yield on both portfolio and S&P500 is 4%. How can portfolio be insured at \$450k (excluding div) over next 3 months?
  - A1: # Puts =
  - A2: Choose  $K=900$ .
- Q: Now suppose portfolio has  $b=2.0$  How can the portfolio (including dividends) be insured at \$455k over next 3 months?
  - A1: # Puts =
  - A2:

# 7 Portfolio Insurance (2)

- A1: # Puts =  $\beta * \$Portfolio / 100S_0 = 2 * 500,000 / (100 * 1,000) = 10$
- A2: Choose K associated with target portfolio value (455k equates to 960).
  - Text ignores div rec'd in target portfolio value, so numbers slightly different

|                         |               |                 |  |                                     |      |
|-------------------------|---------------|-----------------|--|-------------------------------------|------|
|                         | <b>Annual</b> | <b>Periodic</b> |  |                                     |      |
| <b><math>R_f</math></b> | 12%           | 3.0%            |  | <b><math>T_2 - T_1</math> (yrs)</b> | 0.25 |
| <b>Div Index</b>        | 4%            | 1.0%            |  | <b>Multiplier</b>                   | 100  |
| <b>Div Port</b>         | 4%            | 1.0%            |  | <b>Contracts</b>                    | 10   |
| <b><math>S_1</math></b> | 1000          |                 |  | <b>Exercise</b>                     | 960  |
| <b>Portfolio</b>        | \$ 500,000    |                 |  |                                     |      |
| <b><math>b_p</math></b> | 2             |                 |  |                                     |      |

| <b><math>S_2</math></b> | <b>Periodic Return on Index</b> | <b>Return on Index Incl Div <math>R_m</math></b> | <b>Return on Port Incl Div <math>E(R_p)</math> CAPM</b> | <b>Value of Unhedge Portfolio Incl Div</b> | <b>Cash Flow from Hedge (Puts)</b> | <b>Value of Hedged Portfolio Incl Div</b> |
|-------------------------|---------------------------------|--------------------------------------------------|---------------------------------------------------------|--------------------------------------------|------------------------------------|-------------------------------------------|
| 1080                    | 8.0%                            | 9.0%                                             | 15.0%                                                   | 575,000                                    | -                                  | 575,000                                   |
| 1040                    | 4.0%                            | 5.0%                                             | 7.0%                                                    | 535,000                                    | -                                  | 535,000                                   |
| 1000                    | 0.0%                            | 1.0%                                             | -1.0%                                                   | 495,000                                    | -                                  | 495,000                                   |
| 960                     | -4.0%                           | -3.0%                                            | -9.0%                                                   | 455,000                                    | -                                  | 455,000                                   |
| 920                     | -8.0%                           | -7.0%                                            | -17.0%                                                  | 415,000                                    | 40,000                             | 455,000                                   |
| 880                     | -12.0%                          | -11.0%                                           | -25.0%                                                  | 375,000                                    | 80,000                             | 455,000                                   |
| 800                     | -20.0%                          | -19.0%                                           | -41.0%                                                  | 295,000                                    | 160,000                            | 455,000                                   |

## 8 Options: Tips for the Savvy Investor

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- Options are traded on many financial assets.
- Options are risky for uninformed investors.
  - Many option traders are informed investors
  - Wrong position may completely wipe your investment, plus cause additional liability (potentially infinite).
  - Writing “naked” options is rare.
- Options can be used to hedge risks or lock-in gains
  - For many investors, options on ETFs may be useful
  - Some contracts can be thinly traded with quoted prices stale.
- Quotes at <http://www.finance.yahoo.com> and <http://biz.yahoo.com/opt/>
  - ^SPX for SP500 on [finance.yahoo.com](http://www.finance.yahoo.com) ^NDX for Nasdaq 100
  - See also option analyzer.
  - CBOE (index options) - <http://www.cboe.com>
  - ETF Options - <http://www.amex.com>